

# Load profiles analysis for electricity market

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## Abstract

*In the wake of electric power system transition towards smart grids, and the adoption of the electric market schemes, electric utilities are facing the need of a better load profiles understanding for their customers. In this work, some key objectives were addresses, such as definition of the mathematical model for calculating the hourly energy specific, identification of the three target groups for users who have developed consumer profiles, definition of the two types of significant load and assessment of the impact of using consumer profiles on users.*

**Keywords:** *Distribution system, electricity market, load profile.*

## 1. Introduction

In the free market of electricity, electricity suppliers need to have information on the customer electricity consumption evolution in order to buy sufficient energy from the wholesale market to cover the hourly consumption at negotiated prices and average periods [1-15].

In the absence of such information, the service provider will be obliged to purchase the electricity wholesale market. The quantities of purchased energy may be smaller than its customer's needs – in which case, the deficit will be covered by purchasing the missing quantities in the market for next day or balancing market at higher prices. Where the supplier will buy power on the wholesale market more energy than is necessary for the customer, will be forced to sell the surplus, balancing market at a price lower than that with which the energy was purchased [16-36].

For those customers that have implemented smart metering devices (which can record consumption at different time intervals, memorize the values and remotely transmit the information), this consumption variation is known [37-42]. For customers that have not installed such intelligent devices, it requires a method by which the total electricity consumption over a period of time to be assigned to time slots [43,44]. Typically, the issue of the load curve profile determination is posed for small users and for users. In their case, the installation of meters with registration of hourly electricity consumption is economically unjustified [45,46].

## 2. Operational and functional requirements for accurate load profiling – analytical assessment

Average daily consumption which is scheduled by using weights specified in a table which contains data relating to consumer profile (differentiated for working day and non-working day) is defined from the relations detailed in sequel.

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## 2.1 Monthly energy aggregation

For an average month, some using the data presented in a table that contains the results of the measurements of energy for all hourly intervals (curves, as the average consumer used to establish the data measured consumer profile):

$$\bar{Q}_{WD} = q_{WD} * N_{WD} \quad (1)$$

$$\bar{Q}_{NWD} = q_{NWD} * N_{NWD} \quad (2)$$

$$\bar{Q}_{WD} = Q_{WD} + Q_{NWD} \quad (3)$$

where:

$\bar{Q}_{WD}$  = amount of energy distributed on working days for a month, according to the measured values;

$\bar{Q}_{NWD}$  = amount of energy distributed in non-working days for a month, according to the measured values;

$q_{WD}$  = average daily consumption associated with any working days for a month, according to the values given in the table containing the results of the measurements of energy for all hourly intervals;

$q_{NWD}$  = average daily consumption associated with any non-working days for a month, according to the values given in the table containing the results of the measurements of energy for all hourly intervals;

$Q$  = energy distributed within one month according to measured values

$N_{WD}$  = number of working days in the month;

$N_{NWD}$  = number of non-working days in the month

## 2.2 Evaluation of energy weights

$$P_{WD} = \frac{\bar{Q}_{WD}}{Q} \quad (4)$$

$$P_{NWD} = \frac{\bar{Q}_{NWD}}{Q} \quad (5)$$

where:

$P_{WD}$ ,  $P_{NWD}$  is the weight of the energy distributed for one month with respect to working days/holidays, determined accordingly to the measured values which underline the consumer profile, according to the table that contains the results of the measurements of energy for all hourly intervals;

## 2.3 Monthly energy calculation

Energy distributed in the settlement month, differentiated according to type of day (working/nonworking) shall be established according to the following relationship:

$$\bar{Q}_{monthWD} = Q_{month} * P_{WD} \quad (6)$$

$$\bar{Q}_{monthNWD} = Q_{month} * P_{NWD} \quad (7)$$

$$\bar{Q}_{monthWD} + \bar{Q}_{monthNWD} = Q_{month} \quad (8)$$

where:

$Q_{month}$  = the amount of energy distributed in the settlement,

## 2.4 Monthly calculation of energy weights

Daily quantities of energy distributed in paying month must be approved according to profile schedule (using the weights shown in a table containing data relating to consumer profile) is determined according to the relationship presented in sequel:

$$Q_{WD} = \frac{Q_{monthWD}}{N_{WD}} \quad (9)$$

$$Q_{NWD} = \frac{Q_{monthNWD}}{N_{NWD}} \quad (10)$$

## 2.5 Daily/hourly energy calculation

Monthly representation of quantities of energy will be distributed on the basis of the approved profile on differentiated working days / non-working days, according to the following relationship:

a). working day

$$Q_{hourWD} = Q_{WD} * \gamma \quad (11)$$

where:

$Q_{hourWD}$  = energy distributed according to a time interval for a working day;

$\gamma$  = represents the percentage determined for the characteristic profile of working days, for a given time interval (according to the table containing data relating to consumer profile)

b). non-working day

$$Q_{hourNWD} = Q_{NWD} * \eta \quad (12)$$

where:

$Q_{hourNWD}$  = energy distributed according with a time interval for a working day;

$\eta$  = is the percentage determined for the characteristic profile of working day, for a given time interval (according to the table containing the data relating to consumer profile).

Hourly quantities are expressed in, MWh with 3 decimals, so that the difference between the amount of energy distributed monthly and the sum of hourly energies to be less than 1 kWh.

## 3. System application

The question of determining the load curve profile is very economically-efficient for small users and for users. Under these circumstances, the establishment of hourly values of energy associated with a supplier can realize, for each point of consumption for providing hourly consumption by spreading recorded on a calculation based on a consumer profile.

Within current paper, the following consumers were took under consideration:

1. Fuel stations
2. Small businesses without cooling
3. Small businesses with cooling
4. Schools

### 3.1 Fuel stations

This illustrates loading profile contributions such as lighting, cooling, ventilation and other tasks performed throughout the day. Evaluation of total energy consumption in energy will show a rapid increase during the

morning because of the transitional arrangements of the receivers. Once the systems are started, the demand is relatively constant throughout the day.

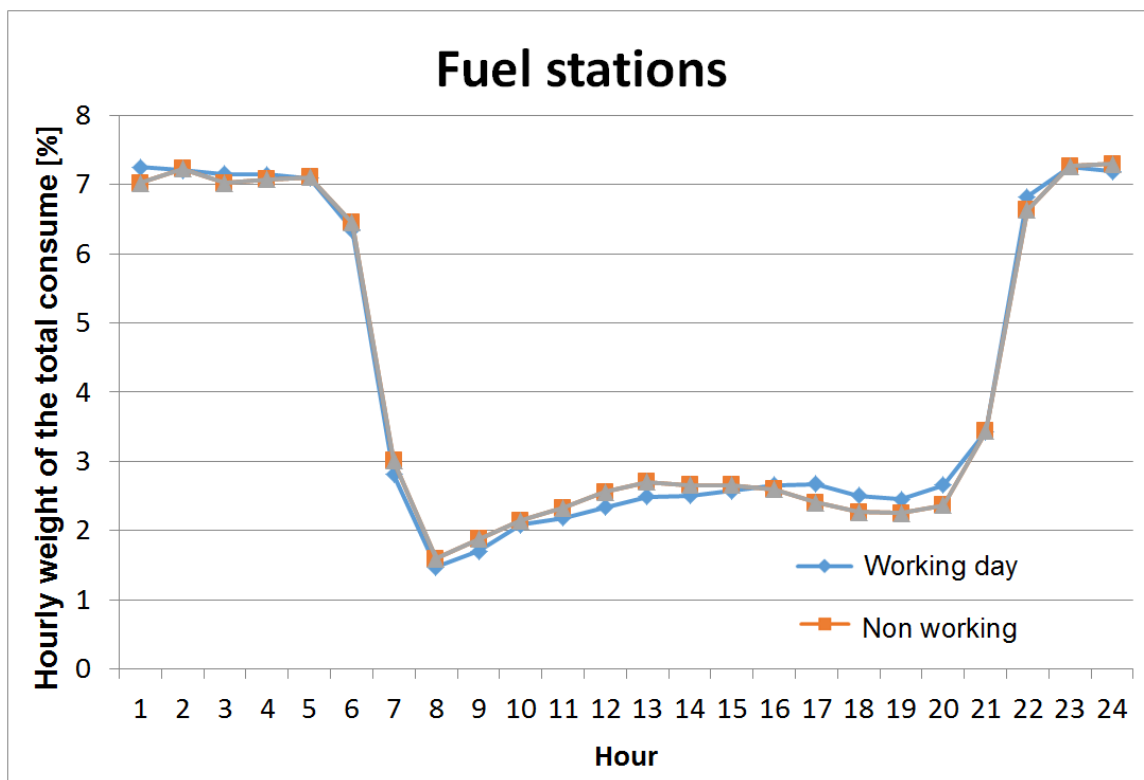


Fig. 1. Load curves for fuel stations

**Table 1 Measurements results**

Average consume curve [MWh]		
Interval	Interval	Interval
00:00:00	0.004292661	0.00403134
01:00:00	0.004293374	0.004025699
02:00:00	0.00431324	0.004067442
03:00:00	0.004339073	0.004211893
04:00:00	0.0043308	0.004205129
05:00:00	0.004474134	0.004150411
06:00:00	0.004486111	0.004113899
07:00:00	0.004406811	0.00390353
08:00:00	0.006805816	0.003982609
09:00:00	0.011768425	0.004847129
10:00:00	0.012067337	0.004919832
11:00:00	0.012192786	0.004936485
12:00:00	0.012029691	0.004917517
13:00:00	0.012074995	0.004672229
14:00:00	0.012670302	0.005389044
15:00:00	0.012493785	0.005340656
16:00:00	0.012752344	0.005375426
17:00:00	0.012025259	0.005502721
18:00:00	0.009438688	0.005893038
19:00:00	0.006964362	0.005928727
20:00:00	0.004961839	0.004721399
21:00:00	0.00419137	0.004045598
22:00:00	0.004175531	0.004062494
23:00:00	0.004159727	0.004051396
Q <sub>WD</sub>	<b>0.185708461</b>	
Q <sub>NWD</sub>		<b>0.111295642</b>

**Table 2 Data for fuel stations (hourly weights of energy consume)**

	Consume profile	
	Mean WD [%]	Mean NWD[%]
00:00:00	2.311505444	3.622190662
01:00:00	2.311889189	3.617122116
02:00:00	2.322586538	3.654628397
03:00:00	2.336497257	3.784418488
04:00:00	2.332042219	3.778340724
05:00:00	2.40922455	3.729176304
06:00:00	2.415674017	3.69636986
07:00:00	2.372972836	3.507352062
08:00:00	3.664785357	3.578405416
09:00:00	6.337043236	4.355183359
10:00:00	6.498000695	4.42050712
11:00:00	6.565552497	4.435469842
12:00:00	6.477728882	4.418427075
13:00:00	6.502124331	4.198033707
14:00:00	6.82268434	4.842098201
15:00:00	6.727633712	4.798620693
16:00:00	6.866862061	4.82986245
17:00:00	6.475342473	4.944237998
18:00:00	5.082529611	5.294940665
19:00:00	3.750158578	5.327007124
20:00:00	2.671843172	4.242213655
21:00:00	2.256962489	3.635000816
22:00:00	2.248433386	3.650182388
23:00:00	2.239923131	3.640210877

### 3.2 Small businesses without cooling

This illustrates loading profile contributions such as lighting, cooling, ventilation and other tasks performed throughout the day. Evaluation of total energy consumption in energy will show a rapid increase during the

morning because of the transitional arrangements of the receivers. Once the systems are started, the demand is relatively constant throughout the day.

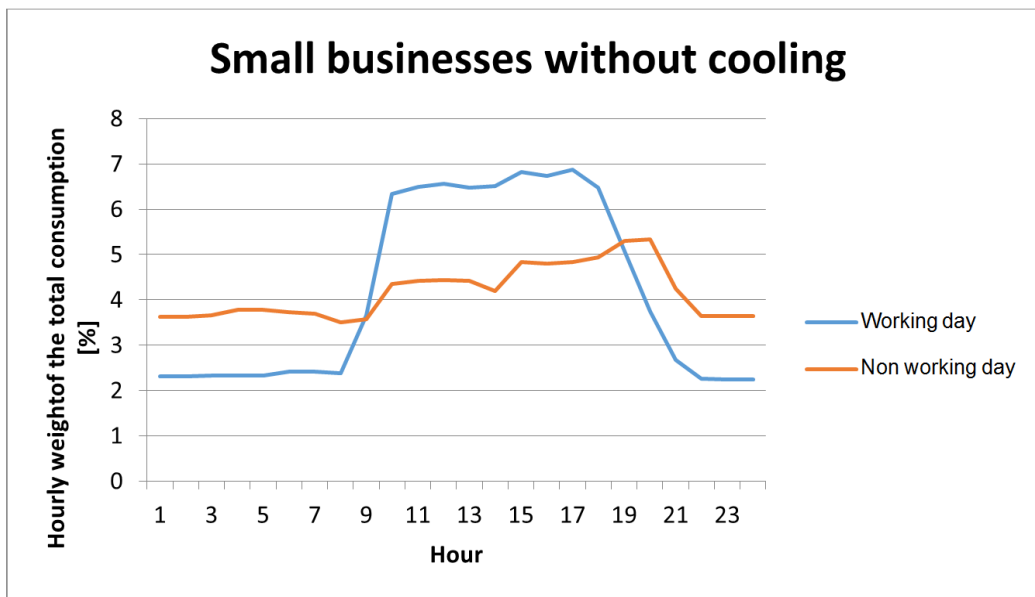


Fig. 2. Load curves for SBwC (WD and NWD) Small businesses with cooling

Minimum and maximum limits presents a limited variation of about 2%, which indicates the uniformity of type SBC users consumption. The load curve flattening we can say that it has a high value which indicates that in the case of SBC have a flat load curve.

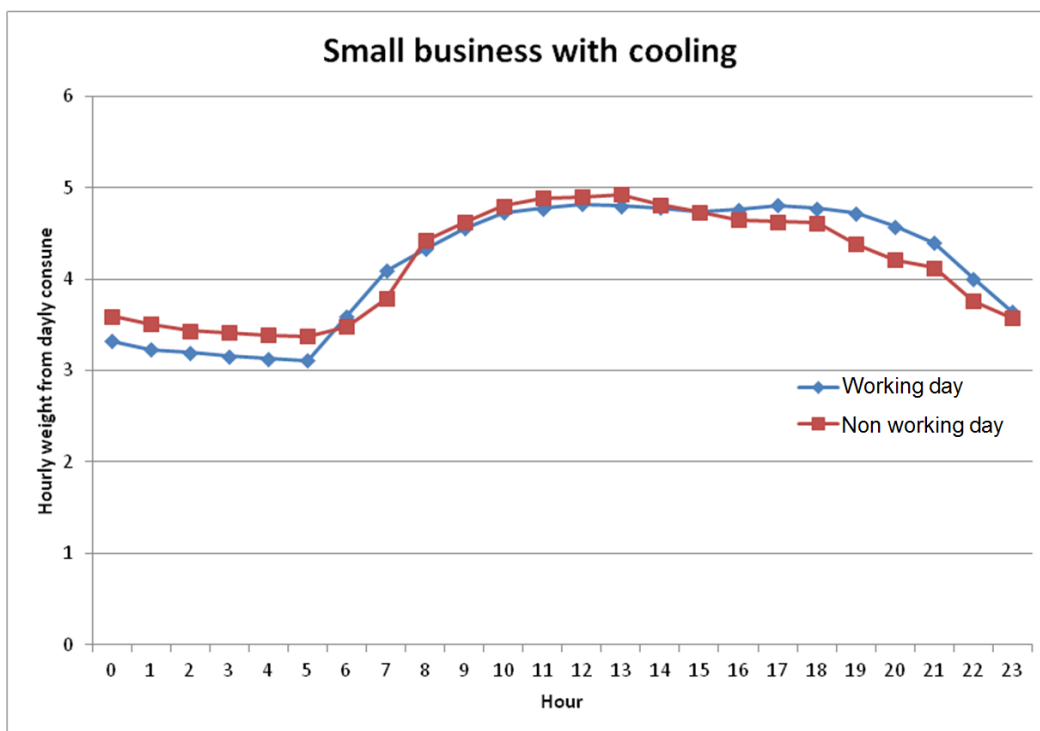
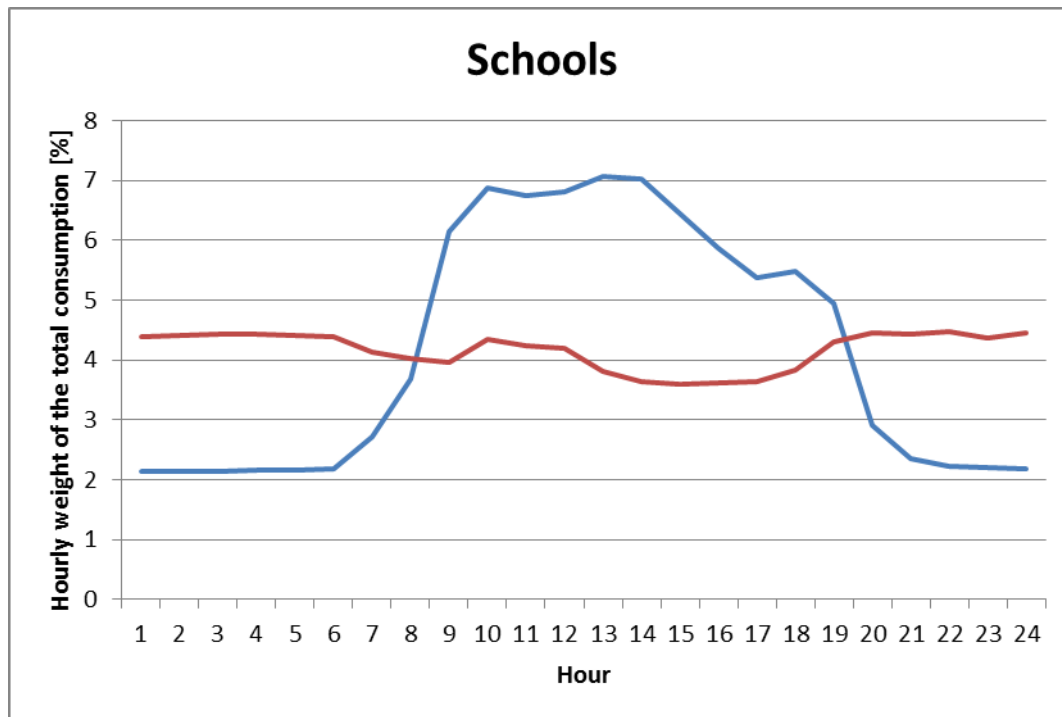


Fig. 3. Load curves for SBC (WD and NWD)



**Fig. 4.** Load curves for Schools

The overall purpose of this section is to reach the final economic target of fully describe the customers' behavior by exactly quantifying their consumption patterns, starting from monthly energy aggregation.

#### 4. Conclusions

In this work, some key objectives were completed, such as definition of the mathematical model for calculating the hourly energy specific, identification of the three target groups for users who have developed consumer profiles, definition of the two types of significant load and assessment of the impact of using consumer profiles on users

Also, throughout the whole paper, the authors have tried to create a framework that can be used later by the beneficiary for mathematical models. In sequel are listed the obstacles in the face of improving energy distribution activity and the action required to be taken with a view to the removal of obstacles.

There are a few issues that pose a serious threat to the future development of electric distribution system. A brief collection of these issues are presented in sequel:

- Lack of investment in facilities for low voltage networks, a significant proportion of the consumers having old installations with access to conductors.
- Poor status of the electric distribution power system, namely network areas with great lengths, LV overload, with inadequate insulation.
- Action to raise awareness of the extent of the economic agents who work with very low loads. Actions required in order to mitigate the upper-mentioned issues:
- Continuance of control actions for faulty consumers of electrical energy,
- Recovery and restoration of the electric power system is compulsory for reaching the goal of having a secure system
- Development of electric distribution systems using economic-based strategies

## References

- [1] Shijie Deng, *Stochastic Models of Energy Commodity Prices and Their Applications: Mean-reversion with Jumps and Spikes*, Program on Workable Energy Regulation (POWER), University of California Energy Institute, PWP-073, February 2000.
- [2] Trueck Stefan, Weron Rafal and Wolff Rodney, *Outlier Treatment and Robust Approaches for Modeling Electricity Spot Prices*, Hugo Steinhaus Center, Wroclaw University of Technology, August 2007, MPRA Paper No. 4711, posted 07. November 2007 / 04:09.
- [3] Adam Misiorek, Stefan Trueck and Rafal Weron, *Point and Interval Forecasting of Spot Electricity Prices: Linear vs. Non-Linear Time Series Models*, Nonlinear analysis of electricity prices, Volume 10, Article 2, Issue 3, 2006.
- [4] Michael Bierbrauer, Stefan Trück, and Rafael Weron, *Modeling Electricity Prices with Regime Switching Models*, M. Bubak et al. (Eds.): ICCS 2004, LNCS 3039, pp. 859–867, 2004. c Springer-Verlag Berlin Heidelberg, 2004.
- [5] Rafał Weron, *Heavy tails and electricity prices*, Research Report HSC/05/2, The Deutsche Bundesbank's Annual Fall Conference, Eltville, 10-12 November 2005.
- [6] Ross Baldick, Sergey Kolos, Stathis Tompaids, *Interruptible Electricity Contracts from an Electricity Retailer's Point of View: Valuation and Optimal Interruption*, Operations Research Vol. 54, No. 4, pp. 627–642, ISSN 0030-364X, EISSN 1526-5463 -06 - 5404 -0627, July–August 2006.
- [7] Min Liu and Felix F. Wu, *Managing Price Risk in a Multimarket Environment*, IEEE Transactions on Power Systems, Vol. 21, No. 4, pag.1512-1219, November 2006.
- [8] Jacob Lemming, *Electricity Price Modelling for Profit at Risk Management*, Systems Analysis Department Risk National Laboratory, DK-4000, Roskilde.
- [9] Siem Jan Koopman, Marius Ooms, M. Angeles Carnero, *Periodic Seasonal Reg-ARFIMA-GARCH Models for Daily Electricity Spot Prices*, TI 2005-091/4 Tinbergen Institute Discussion Paper, September 16, 2005.
- [10] Alvaro Cartea and Marcelo G. Figueroa, *Pricing in Electricity Markets: a mean reverting jump diffusion model with seasonality*, September 2, Commodities Modelling Workshop, Birkbeck College, University of London, September 2004.
- [11] Reinaldo C. Garcia, Javier Contreras, Marco van Akkeren and João Batista C. Garcia, *A GARCH Forecasting Model to Predict Day-Ahead Electricity Prices*, IEEE Transactions On Power Systems, Vol. 20, No. 2, May 2005.
- [12] Derek W. Bunn, *Structural and Behavioural Foundations of Competitive Electricity Prices*, Modelling Prices in Competitive Electricity Markets, Edited by D.W. Bunn. John Wiley & Sons, Ltd. ISBN 0-470-84860-X, 2004.
- [13] Terence C Mills, *The economic modelling of financial time series*, Second edition, Cambridge University Press, 1999.
- [14] Julián Barquín, Ángel Garro, Eugenio Fco. Sánchez-Úbeda, Santiago Tejero, *A New Model for Electricity Price Series Modelling and Forward and Volatility Curves Computation*, 8th International Conference on Probabilistic Methods Applied to Power Systems, Iowa State University, Ames, Iowa, September 12-16, 2004.
- [15] Eva Benz, Stefan Trück, *Modeling the Price Dynamics of CO<sub>2</sub> Emission Allowances*, Preprint submitted to Elsevier Science February 20, 2008.
- [16] Geman, H. and Roncoroni, A., *Understanding the fine structure of electricity prices*, Journal of Business 79 (3) 1225-1261, 2006.
- [17] Svetlana Borovkova, Ferry Jaya Permana, *Modelling electricity prices by the potential jump-diffusion*, Stochastic Finance 2004 Autumn School & International Conference, 2004.
- [18] Audun Botterud, Magnus Korpas, *A stochastic dynamic model for optimal timing of investments in new generation capacity in restructured power systems*, Electrical Power and Energy Systems 29, 163–174, 2007.
- [19] Nektaria V. Karakatsani and Derek W. Bunn, *Modelling the Volatility of Spot Electricity Prices*, Department of Decision Sciences, London Business School, March 2004.
- [20] Hanjie Chen and Ross Baldick, *Optimizing Short-Term Natural Gas Supply Portfolio for Electric Utility Companies*, IEEE Transactions on Power Systems, Vol. 22, No. 1, February 2007.
- [21] Nima Amjadi and Farshid Keynia, *Day-Ahead Price Forecasting of Electricity Markets by Mutual Information Technique and Cascaded Neuro-Evolutionary Algorithm*, IEEE Transactions On Power Systems, Vol. 24, No. 1, February 2009.
- [22] Work Package 5 – D5.2, *Modelling electricity prices: from the State of the Art to a draft of a new proposal*, Project contract no. 043363, January 2007.
- [23] Matt Davison, C. Lindsay Anderson, Ben Marcus, and Karen Anderson, *Development of a Hybrid Model for Electrical Power Spot Prices*, IEEE Transactions On Power Systems, Vol. 17, No. 2, May 2002.
- [24] Antonio J. Conejo, Miguel A. Plazas, Rosa Espinola, and Ana B. Molina, *Day-Ahead Electricity Price Forecasting Using the Wavelet Transform and ARIMA Models*, IEEE Transactions On Power Systems, Vol. 20, No. 2, May 2005.
- [25] Shi-Jie Deng, Wenjiang Jiang, *Levy process-driven mean-reverting electricity price model: the marginal distribution analysis*, Elsevier, available online 10 July 2004.
- [26] Terry A. Robinson, *Electricity pool prices: a case study in nonlinear time-series modelling*, Applied Economics, 32, 527- 532, 2000.
- [27] Graeme A. Guthrie and Steen Videbeck, *Electricity Spot Price Dynamics: Beyond Financial Models*, New Zealand Institute for the Study of Competition and Regulation, and Victoria University of Wellington December 14, 2004.
- [28] Ronald Huisman, Christian Huurman, Ronald Mahieu, *Hourly electricity prices in day-ahead markets*, Energy Economics 29, 240–248, 2007.
- [29] Mika Goto, G. Andrew Karolyi, *Understanding Electricity Price Volatility Within and Across Markets*, JEL Classification Codes: G13, August 25, 2003.
- [30] Helen Higgs, Andrew C. Worthington, *Stochastic price modelling of high volatility, mean-reverting, spike-prone commodities: The Australian wholesale electricity market*, JEL classification: C32, D40, Q40;
- [31] Rafal Weron, *Heavy-tails and regime-switching in electricity prices*, Mathematical Methods of Operations Research manuscript, 9 May 2008.
- [32] Thilo Meyer-Brandis, Peter Tankov, *Multi-factor jump-diffusion models of electricity prices*, project supported by the Europlace Institute of Finance.
- [33] Jan Seifert, Marliese Uhrig-Homburg, *Modelling Jumps in Electricity Prices: Theory and Empirical Evidence*, JEL Classification: C11, G12, G13, Q4.
- [34] D. C. Sansom, T. Downs and T. K. Saha, *Support Vector Machine Based Electricity Price Forecasting For Electricity Markets utilising Projected Assessment of System Adequacy Data*, The Sixth International Power Engineering Conference (IPEC2003), 27-29, Singapore, November 2003.
- [35] Stephan Schlueter, *A long-term/short-term model for daily electricity prices with dynamic volatility*, Energy Economics 32, 1074–1081, 2010.
- [36] Michel Culot, Valerie Goffin, Steve Lawford, Sebastien de Menten and Yves Smeers, *An Affine Jump Diffusion Model for Electricity*, Department of Mathematical Engineering and CORE, UCL, January 7, 2006.
- [37] Ronald Huisman, Ronald Mahieu, *Regime jumps in electricity prices*, Energy Economics 25, 425–434, 2003.
- [38] Qin Zhang and Xifan Wang, *Hedge Contract Characterization and Risk-Constrained Electricity Procurement*, IEEE Transactions On Power Systems, Vol. 24, No. 3, August 2009.
- [39] Chang R.F., Lu C.N., *Load Profiling and Its Applications in Power Market*, PES, Toronto, rap. 000686, 2003.
- [40] Gerbec D.š.a., *Consumers' Load Profile Determination Based on Different Classification Methods*, PES, Toronto, rap. 000797, 2003.
- [41] Gerbec G., Gubina F., Toroš Z., *Actual Load Profiles of Consumers without Real Time Metering*, PESGM, San Francisco, rap. 000841, 2005.
- [42] Grigoras G.š.a., *Missing Data Treatment of the Load Profiles in Distribution Networks*, IEEE PowerTech Bucharest, rap.782, 2009.



- [43] Ilie I-S., Chicco G., *Exploiting Support Vector Clustering Techniques for Electrical Load Profiling*, MPS, Cluj-Napoca, III.9 Hesaminia A. – 59.pdf, 2008.
- [44] Ramos S., Vale Z., *Data Mining Techniques to Support the Classification of MV Electricity Customers*, PESGM, Pittsburgh, rap.001209, 2008
- [45] Salgado R.M., Ohishi T., Ballini R., *Clustering Bus Load Curves*, PSCE, New York, rap. 000581, 2004.
- [46] Sousa J.C., Neves L.P., Jorge H.M., *Determining typical load profiles of Low Voltage Consumers*, IYCE Conference, Budapesta, rap. 176, 2007